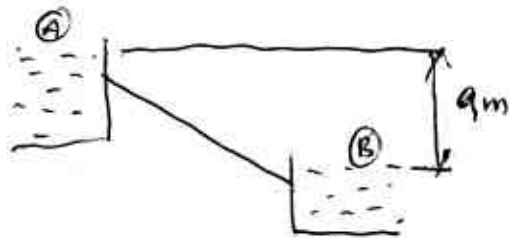


Tutorial



- 1) given:-
 $d = 400 \text{ mm}$
 $l = 1.7 \text{ km}$
 $ele = 9 \text{ m}$
 $\mu = 1.141 \times 10^{-6} \text{ m}^2/\text{s}$

a) Commercial steel

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{losses}_{(A-B)}$$

$$z_A - z_B = \sum \text{losses}_{(A-B)}$$

$$9 \text{ m} = \left(\frac{f l}{d}\right) \frac{V^2}{2g} \quad \text{--- (1)}$$

$$9 = \left(\frac{16 f l}{2g \pi^2 d^5}\right) Q^2$$

used (1)

$$\frac{9(2g)}{V^2} = \frac{f l}{d}$$

$$\frac{(9)(2g)(d)}{V^2 l} = f$$

$$Q_{\text{max}} = \left(\frac{9(2g)(d)}{V^2 l}\right) l \left(\frac{V^2}{2g}\right)$$

$$Q = AV$$

$$Re = \frac{\rho V d}{\mu}$$

$$f = 0$$

$$Q = \frac{\pi d^2}{4} (V)$$

$$Q = 0.126 \text{ m}^3/\text{s}$$

$$Q = 0.126 \text{ m}^3/\text{s}$$

$$\frac{(9)d}{V^2} = 0$$

$$9 = \frac{16 f l}{2g \pi^2 d^5} (0.018)$$

=

$$V = \frac{4Q}{\pi d^2}$$

$$V = 7.96 \text{ m/s}$$

Guess $f = 1$

$$q = \frac{fL}{4} \left(\frac{V^2}{2g} \right) \quad \text{--- (1)}$$

$$q_m = \frac{(1)(1700)}{0.4} \cdot \frac{V^2}{2g}$$

$$V^2 = \cancel{17} 0.042$$

$$V^{th} = 0.204 \text{ m/s}$$

$$Re = \frac{\rho v d}{\mu}$$

$$Re = \frac{(1000)(0.204)(0.4)}{1.141 \times 10^{-6}}$$

$$Re = 7.15 \times 10^7$$

(f) actual for commercial steel.

$$\epsilon/d = \frac{0.152 \times 10^{-3}}{0.4} = 0.00038$$

$$Re = 7.15 \times 10^7$$

$$f = 0.011$$

$$\therefore V^2 = \frac{(9)(0.4)(2g)}{0.011(1700)}$$

$$V^2 = 3.78$$

$$V = 1.943 \text{ m/s}$$

$$\begin{aligned} Q &= AV \\ &= \frac{\pi d^2}{4} (1.943) \\ Q &= 0.244 \text{ m}^3/\text{s} \end{aligned}$$

f actual for Cast iron.

$$Re = 7.15 \times 10^7$$

$$f = 0.0135$$

$$V^2 = \frac{(9)(0.4)(29)}{0.0135(1700)}$$

$$V = 1.754 \text{ m/s}$$

$$Q = A V$$
$$= \left(\frac{\pi d^2}{4} \right) (1.754)$$

$$Q = 0.22 \text{ m}^3/\text{s}$$

f actual for Smooth concrete.

$$\epsilon/d = 0.002$$

$$Re = 7.15 \times 10^7$$

$$f = 0.023$$

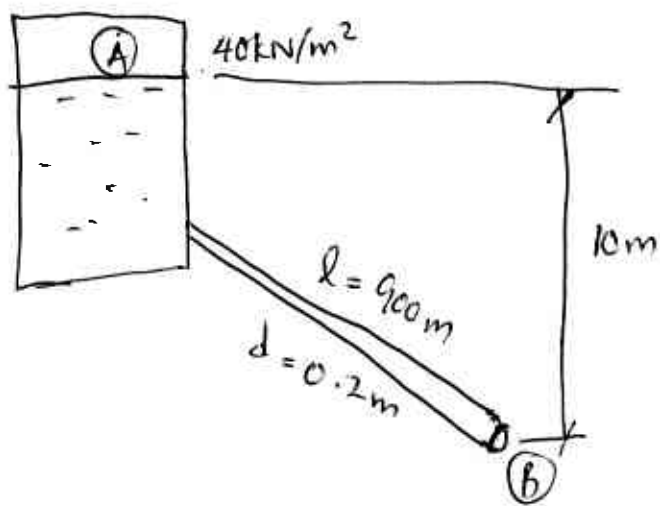
$$V^2 = \frac{\cancel{(0.023)}(9)(0.4)(29)}{(0.023)(1700)}$$

$$V^2 = 1.806$$

$$V = 1.344 \text{ m/s}$$

$$Q = \frac{\pi d^2}{4} (1.344)$$

$$Q = 0.169 \text{ m}^3/\text{s} \#$$



Condition ①

$$Q_B = 49 \text{ l/s} = 0.049 \text{ m}^3/\text{s}$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{losses}$$

$$\begin{aligned} \frac{P_A}{\rho g} &= (z_B - z_A) + \sum \text{loss}_{A-B} \\ &= (0 - 10) + \sum \text{loss}_{(A-B)} \end{aligned}$$

$$\left(\frac{40 \times 10^3}{9810} \right) + 10 = \sum \text{loss}$$

$$14.08 = \sum \text{loss}$$

$$14.08 = \left(\frac{f l}{d} \right) \left(\frac{V^2}{2g} \right)$$

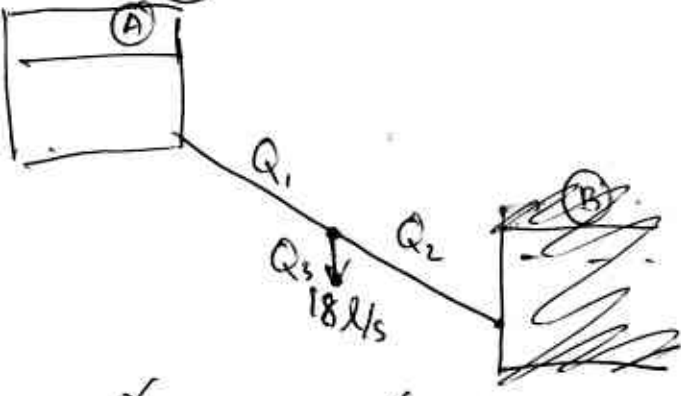
$$14.08 = \left(\frac{f l}{2g \rho^2 d^5} \right) Q^2$$

$$f = \frac{(14.08)(2g \rho^2 d^5)}{Q^2 (l)}$$

$$f = 0.0198$$

*

dition (2)



$$Q_1 = 0.049 \text{ m}^3/\text{s}$$

$$Q_2 =$$

$$Q_3 = 0.018 \text{ m}^3/\text{s}$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum_{\text{losses}} (A-B) \quad Q_2 = 0.049 - 0.018 = 0.031$$

$$\frac{P_A}{\rho g} + (z_A - z_B) = \sum_{\text{losses}} (A-B)$$

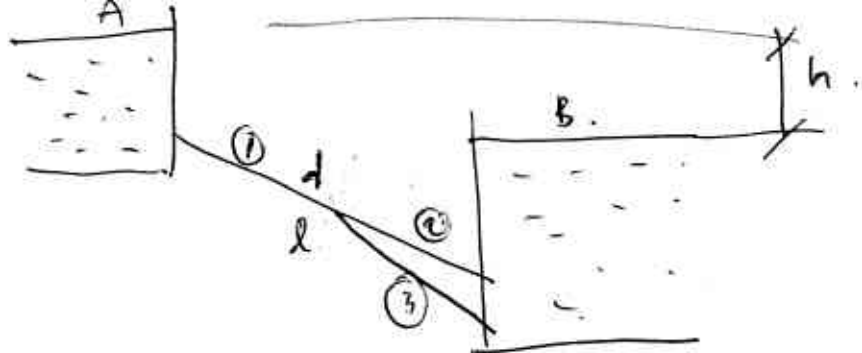
$$\frac{P_A}{\rho g} + 10 = \left(\frac{16 f l}{2g \pi^2 d^5} \right) Q^2$$

$$\frac{P_A}{\rho g} = \frac{16 (0.0198) (900)}{2g (\pi^2) (0.2)^5} Q^2$$

$$P_A = 1.4 \text{ MN/m}^2$$

#

5)



$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{Loss}$$

$$\sum \text{Loss}_{A-B} = (z_A - z_B)$$

$$\sum \text{Loss}_{(A-B)} = (\Delta h)$$

$$\left(\frac{16fl}{29\pi^2 d^5} \right) Q^2 = \frac{\Delta h}{\frac{h 29\pi^2 d^5}{16fl}}$$

$$l = \frac{l}{2}$$

$$Q_1 = Q_2 + Q_3$$

$$Q_1 = 2Q_2 = Q_2 = \frac{1}{2}Q_1$$

$$h_{\text{Loss} \textcircled{2}} = h_{\text{Loss} \textcircled{3}} = \left(\frac{16fl}{29\pi^2 d^5} \right) Q^2$$

$$\boxed{\sum \text{Loss}_{(A-B)} = kQ_1^2 + kQ_2^2} = \left(\frac{16fl}{49\pi^2 d^5} \right) Q^2$$

$$\therefore \sum \text{Loss}_{A-B} = (z_A - z_B)$$

$$\sum \text{Loss} = \left(\frac{16fl/2}{29\pi^2 d^5} \right) Q_1^2 + \left(\frac{16fl/2}{29\pi^2 d^5} \right) Q_2^2$$

$$\Delta h = \left(\frac{16fl/2}{29\pi^2 d^5} \right) (Q_1^2 + Q_2^2)$$

$$= \frac{16fl/2}{29\pi^2 d^5} (Q_1 + \frac{1}{2}Q_1)^2$$

$$\Delta h = \left(\frac{16 f l / 2}{29 H^2 d^5} \right) \left(\frac{3}{2} Q_1 \right)$$

$$Q_1^2 = \frac{(29 H^2 d^5) (\Delta h)}{16 f l / 2} \left(\frac{2}{3} \right)$$

∴ increase discharge.

$$= \frac{Q_1 \text{ condition ①}}{Q_1 \text{ condition ②}} \times 100$$

$$\frac{\left(\frac{29 H^2 d^5}{16 f l} \right) (\Delta h)}{\left(\frac{49 H^2 d^5}{16 f l} \right) (\Delta h) \frac{2}{3}}$$

$$= \frac{\left(\frac{29 H^2 d^5}{16 f l} \right) (\Delta h)}{\left(\frac{49 H^2 d^5}{16 f l} \right) (\Delta h) \frac{2}{3}}$$

$$\frac{1}{2} \times \frac{3}{2} =$$

$$\frac{29 H^2 d^5}{16 f l} \cdot (\Delta h) \frac{2}{3}$$

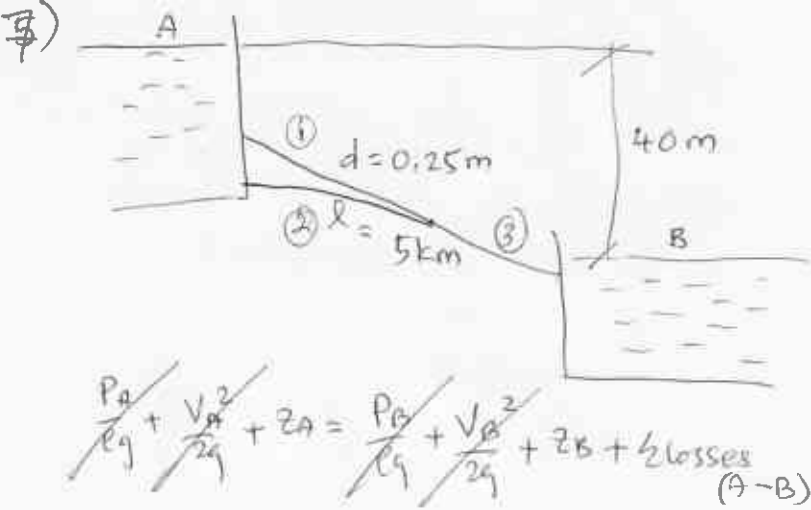
$$= \frac{1}{4} \times \frac{3}{2}$$

$$= \frac{3}{4} \times 100$$

∴ Q_0 condition ①

$\frac{75}{100}$ of Q_1 condition ② = 75% increase. #

∴ increase 25% #



$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{losses}_{(A-B)}$$

$$z_A - z_B = \sum \text{losses}_{(A-B)}$$

$$40 = \sum \text{loss}_{(A-B)}$$

$$40 = KQ^2$$

a) $Q_1 + Q_2 = Q_3$

$$Q_3 = Q_1 + Q_2$$

$$Q_3 = 2Q_1$$

$$\therefore 40 = KQ_1^2 + KQ_3^2$$

$$40 = \left(\frac{16f_1 L_1}{2g \pi^2 d^5} \right) Q_1^2 + \left(\frac{16f_2 L_2}{2g \pi^2 d^5} \right) Q_3^2$$

$$40 = 2009.5 Q_1^2 + 2009.5 Q_3^2$$

$$40 = 2009.5 Q_1^2 + 2009.5 (2Q_1)^2$$

$$40 = 6028.47 Q_1^2$$

$$Q_1 = 0.0815 \text{ m}^3/\text{s}$$

$$\Rightarrow 40 = \left(\frac{16fL}{2g \pi^2 d^5} \right) Q^2$$

$$40 = \left(\frac{fL}{2g \pi^2 d} \right) \frac{V^2}{2g}$$

assume $f = 1 =$

$$40 = \left(\frac{5000}{0.25} \right) \frac{V^2}{19.62}$$

$$V^2 = 0.198 \text{ m/s}$$

$$Re = \rho V d / \mu = 1.141 \times 10^6$$

$$2Re = 6.95 \times 10^8 \quad 4.98 \times 10^7$$

assume smooth pipe.

$$f = 0.0095$$

\therefore Actual =

$$40 = \frac{(0.0095)(5000)}{0.25} \left(\frac{V^2}{2g} \right)$$

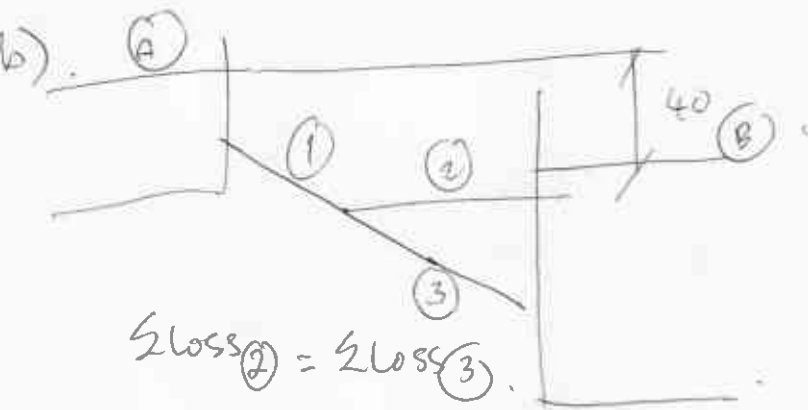
$$V = 2.032 \text{ m/s}$$

$$Q = \left(\pi d^2 / 4 \right) V$$

$$Q_1 = 0.0998 \text{ m}^3/\text{s}$$

$$Q_3 = 2Q_1$$

$$Q_3 = 0.163 \text{ m}^3/\text{s}$$



$$\sum \text{Loss}_{(2)} = \sum \text{Loss}_{(3)}$$

$$\sum \text{Loss} = K Q_2^2$$

$$\sum \text{Loss} = \left(\frac{16 f_2 L_2}{2g \pi^2 d^5} \right) Q_2^2$$

$$f = 0.0095$$

$$\sum \text{Loss}_{(2)} = \left(\frac{16 (0.0095) (2500)}{2g \pi^2 d^5} \right) Q_2^2$$

$$\sum \text{Loss}_{(2)} = 2.072.94 Q_2^2$$

$$40 = 2072.94 Q_1^2 + 2072.94 Q_2^2$$

$$40 = 2072.94 Q_1^2 + 2072.94 Q_1^2$$

$$40 = 2072.94 Q_1^2 + 1036.47 Q_1^2$$

$$40 = 3109.41 Q_1^2$$

$$Q_1^2 = 0.0129$$

$$Q_1 = 0.1134 \text{ m}^3/\text{s}$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{Losses}_{(A-B)}$$

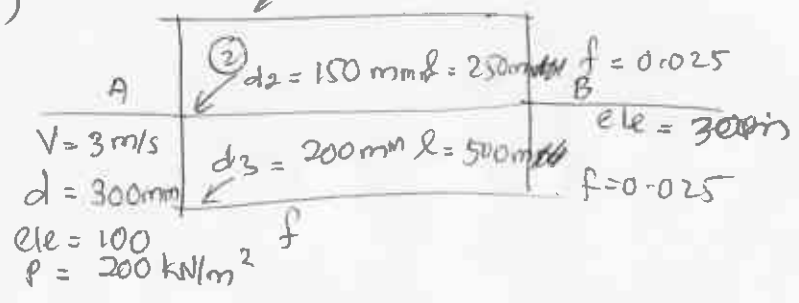
$$(z_A - z_B) = \sum \text{Loss}_{(A-B)}$$

$$40 = K Q_1^2 + K Q_2^2$$

$$Q_1 = Q_2 + Q_3$$

$$Q_1 = 2Q_2$$

a) $\textcircled{1} d_1 = 100 \text{ mm}, l = 300 \text{ mm}, f = 0.025$



$$Q_A = \left(\frac{\pi d^2}{4}\right) V$$

$$Q_A = 0.212 \text{ m}^3/\text{s}$$

$$Q_A = Q_1 + Q_2 + Q_3$$

$$\sum H_{L\textcircled{1}} = \sum H_{L\textcircled{2}} = \sum H_{L\textcircled{3}}$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{Losses}_{(A \rightarrow B)}$$

Guess discharge through pipe $\textcircled{1}$.

$$Q_1' = 0.06 \text{ m}^3/\text{s} \quad V = \frac{4Q}{\pi d^2}$$

$$\sum \text{loss}_{A \rightarrow B} = \left(\frac{16fl}{2g\pi^2 d^5}\right) Q_1'^2 \quad V = 7.64 \text{ m/s}$$

$$= \frac{16(0.025)(300)}{2g\pi^2(0.1)^5} (0.06)^2$$

$$\sum \text{loss}_{A \rightarrow B} = 223.093$$

$$\sum \text{loss}_{A \rightarrow B} = \left(\frac{fl}{d}\right) \frac{V^2}{2g}$$

$$= \frac{(0.025)(300)}{(0.1)(19.62)} (7.64)^2$$

$$\sum \text{loss}_{A \rightarrow B} = 223.09$$

Pipe $\textcircled{2}$

$$223.09 = \frac{fl}{d} \frac{V^2}{2g}$$

$$223.09 = \frac{(0.025)(250)}{(0.15)(19.62)} V^2$$

$$V_2' = 10.25 \text{ m/s}$$

$$Q_2' = \left(\frac{\pi d^2}{4}\right) 10.25 = 0.181 \text{ m}^3/\text{s}$$

Pipe (3):

$$223.09 = \left(\frac{fL}{d}\right) \frac{V^2}{2g}$$

$$223.09 = \frac{0.025 \left(\frac{500}{0.25}\right) V^2}{(0.2)(19.62)}$$

$$V_3 = 8.37 \text{ m/s.}$$

$$Q_3' = \left(\frac{\pi d^2}{4}\right) V$$

$$Q_3' = 0.263 \text{ m}^3/\text{s}$$

get a ratio Q_1'/Q_2'

$$Q_1 = \left(\frac{Q_1'}{Q_1' + Q_2' + Q_3'}\right) Q_A$$

$$Q_1 = \left(\frac{0.06}{0.504}\right) (0.212)$$

$$Q_1 = 0.0252 \text{ m}^3/\text{s}$$

$$Q_2 = \left(\frac{0.181}{0.504}\right) 0.212$$

$$= 0.0761 \text{ m}^3/\text{s}$$

$$Q_3 = \left(\frac{0.263}{0.504}\right) 0.212$$

$$Q_3 = 0.111 \text{ m}^3/\text{s}$$

$$V_1 = \frac{4Q}{\pi d^2} = 3.21 \text{ m/s}$$

$$V_2 = \frac{4Q}{\pi d^2} = 4.31 \text{ m/s}$$

$$V_3 = \frac{4Q}{\pi d^2} = 3.53 \text{ m/s}$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{loss}$$

$$\frac{P_A - P_B}{\rho g} = (z_B - z_A) + \sum \text{loss}_{A \rightarrow B}$$

$$Q_1 = 0.0252 \text{ m}^3/\text{s}$$

$$\sum \text{loss}_{A \rightarrow B} = K Q^2$$

$$= \left(\frac{16fL}{2g\pi^2 d^5}\right) Q_1^2$$

$$= 386.058$$

$$\therefore \frac{P_A - P_B}{\rho g} = -70 + 386.058$$

$$\frac{P_A - P_B}{\rho g} = 316.06$$

Use $\sum \text{loss} = \frac{fL}{d} \left(\frac{V^2}{2g}\right)$

Pipe (1):

$$\frac{P_A - P_B}{\rho g} = (z_B - z_A) + \sum \text{Losses}_{A \rightarrow B}$$

$$\frac{P_A - P_B}{\rho g} = (30 - 100) + \frac{fL}{d} \left(\frac{V^2}{2g}\right)$$

$$\frac{P_A - P_B}{\rho g} = -70 + 39.4$$

$$\frac{P_A - P_B}{\rho g} = -30.6$$

check for Pipe (2):

$$\frac{P_A - P_B}{\rho g} = (30 - 100) + \frac{fL}{d} \left(\frac{V^2}{2g}\right)$$

$$\frac{P_A - P_B}{\rho g} = -70 + 39.4$$

Thus,

$$\frac{P_A - P_B}{\rho g} = -70 + 39.4$$

$$P_A - P_B = (-30.61) 9810$$

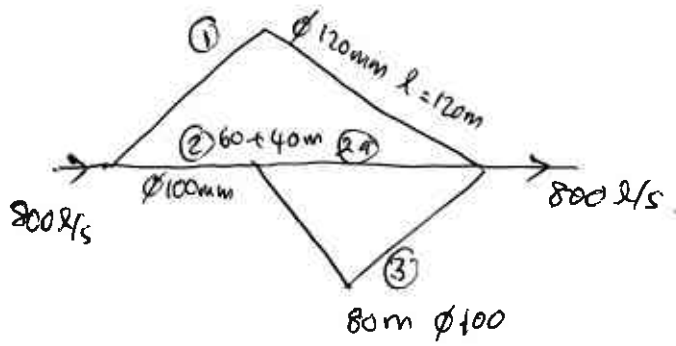
$$P_A - P_B = -300.2841$$

$$- P_B = -300.28 - 200$$

$$- P_B = -500.28 \text{ kN/m}^2$$

$$P_B = 500.28 \text{ kN/m}^2$$

#



f = from moody chart.

Pipe 1 = $f = 0.0135$ for cast iron.

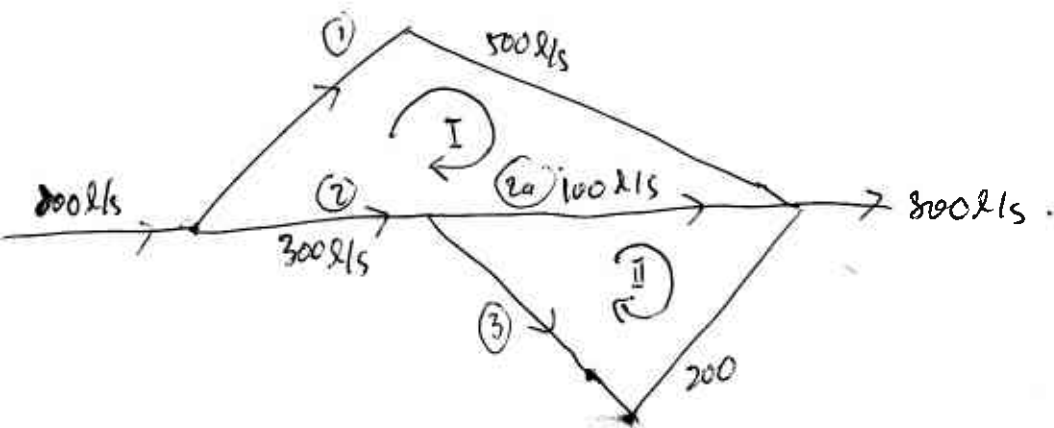
$$k_1 = \frac{16fl}{29H^2d^5} = \frac{16(0.0135)(120)}{29H^2d^5} = \cancel{13385.55} 5379.35$$

$$k_2 = \frac{16fl}{29H^2d^5} = \frac{16(0.0135)(60)}{29H^2(0.1)^5} = 4693$$

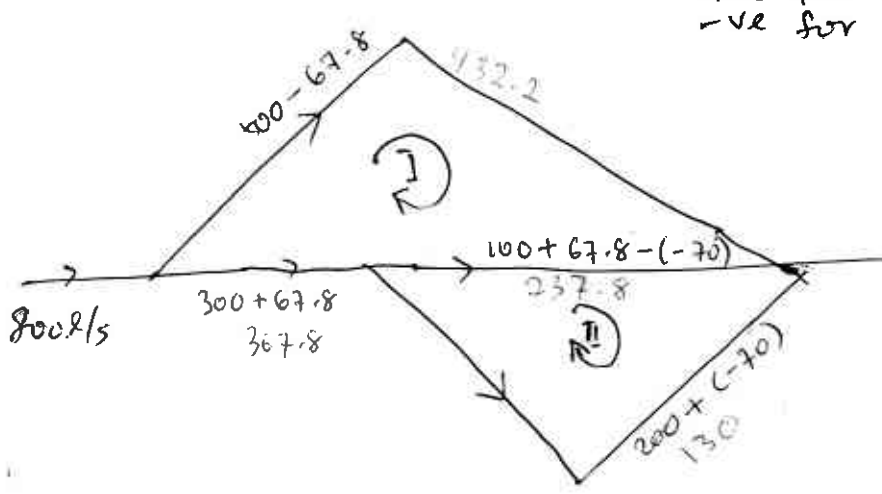
$$k_{2a} = \frac{16fl}{29H^2d^5} = \frac{16(0.0135)(40)}{29H^2(0.1)^5} = 4462$$

$$k_3 = \frac{16fl}{29H^2d^5} = \frac{16(0.0135)(80)}{29H^2(0.1)^5} = 8923.7$$

$$\delta Q = \frac{\sum k_c Q_c^2 - \sum k_{cc} Q_{cc}}{2(\sum k_c Q_c + \sum k_{cc} Q_{cc})}$$



loop	Pipe	$\frac{1}{2} k_c Q_c^2 - \frac{1}{2} k_{cc} Q_{cc}^2$	$2 \frac{1}{2} k_c Q_c + \frac{1}{2} k_{cc} Q_{cc}$
I	①	$(5379.4) \frac{(500)^2}{1000} = 1344.85$	$2(5379.4)(0.5) = 5379.4$
	②	$-(6693) \frac{(300)^2}{1000} = -602.37$	$2(6693)(0.3) = 4015.8$
	③	$-(4462) (0.1)^2 = -44.62$	$2(4462)(0.1) = 892.4$
		697.86	10287.6
			$\delta Q = \frac{697.86}{10287.6}$
			$\delta Q = 0.0678 \text{ m}^3/\text{s} @ 67.8 \text{ l/s}$
II	2a	$(4462) (0.1)^2 = 44.62$	$2(4462)(0.1) = 892.4$
	3	$-(8423.7) (0.2)^2 = -356.95$	$2(8423.7)(0.2) = 3569.48$
		-312.33	4461.88
			$\delta Q = \frac{-312.33}{4461.88} = -0.07 \text{ m}^3/\text{s}$
			@ -70 l/s

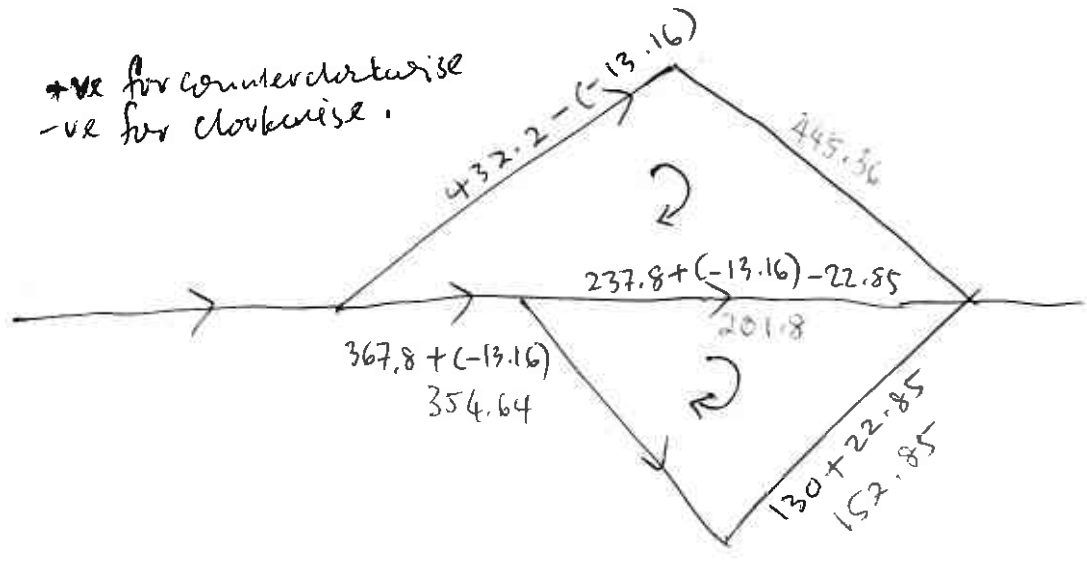


+ve for counterclockwise
-ve for clockwise.

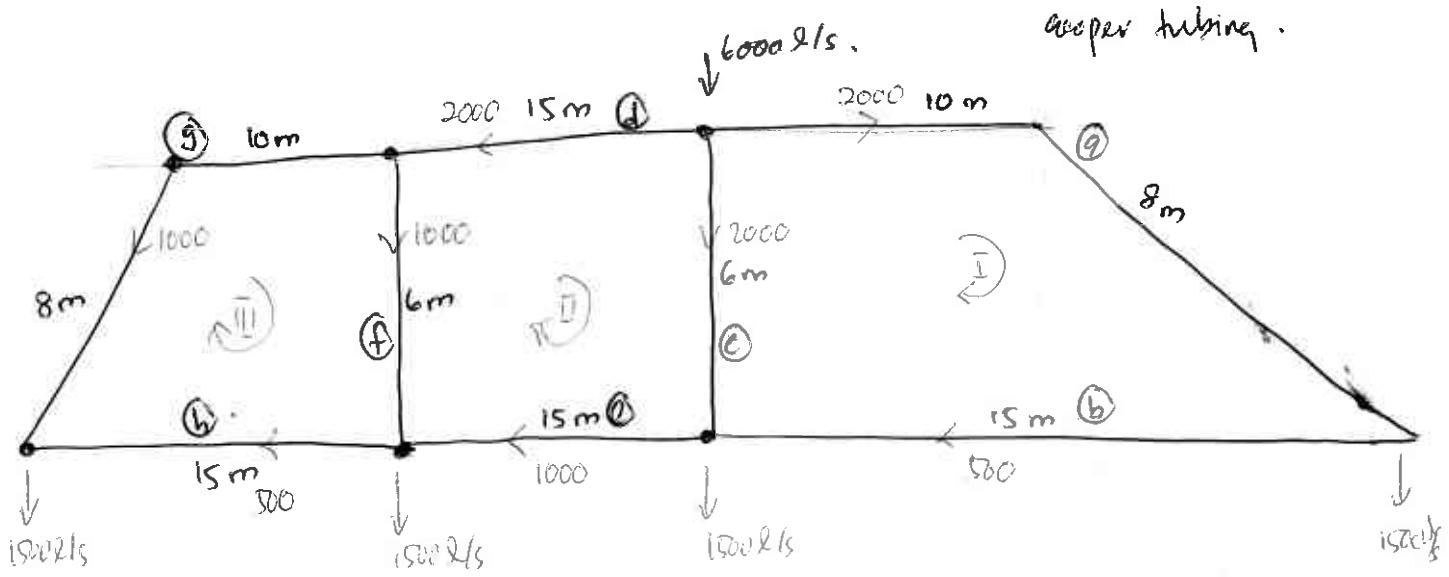
Correction

loop	Pipe	$\frac{1}{2} K Q_c^2 - \frac{1}{2} K C Q_{cc}^2$	$2 \frac{1}{2} K Q_c^2 + \frac{1}{2} K C Q_{cc}^2$
I	①	$(5374.4) \left(\frac{432.2}{1000} \right)^2 = 1003.93$	$2(5374)(0.432) = 4643.14$
	②	$-(6693) \left(\frac{367.8}{1000} \right)^2 = -905.41$	$2(6693)(0.3678) = 4923.4$
	24	$-4462 \left(\frac{0.2378}{1000} \right)^2 = -252.32$	$2(4462)(0.2378) = 2122.13$
		-153.8	11688.67
			$\delta Q = \frac{153.8}{11688.67} = -0.0132 \text{ m}^3/\text{s}$ ② -13.16 l/s
II	24	$+4462 (0.2378)^2 = 252.32$	$2(4462)(0.2378) = 2122.13$
	3	$-(8923) (0.13)^2 = -1508$	$2(8923)(0.13) = 2319.98$
		101.52	4442.11
			$\delta Q = \frac{101.52}{4442.11} = 0.0229 \text{ m}^3/\text{s} \text{ @ } 22.85 \text{ l/s}$

+ve for counter clockwise
-ve for clockwise.



3.



from moody chart
 f for cooper is 0.008

K value for each branch.

$$k_g, k_a = \frac{16fl}{29\pi^2 d^5} = \frac{16(0.008)(18)}{29\pi^2(0.075)^5} = 5014$$

$$k_b, k_d, k_h = \frac{16fl}{29\pi^2 d^5} = \frac{16(0.008)(15)}{29\pi^2(0.075)^5} = \frac{1.92}{4.595 \times 10^{-4}} = 4178.5$$

$$k_c = k_f = \frac{16fl}{29\pi^2 d^5} = \frac{16(0.008)(6)}{4.595 \times 10^{-4}} = 1671.38$$

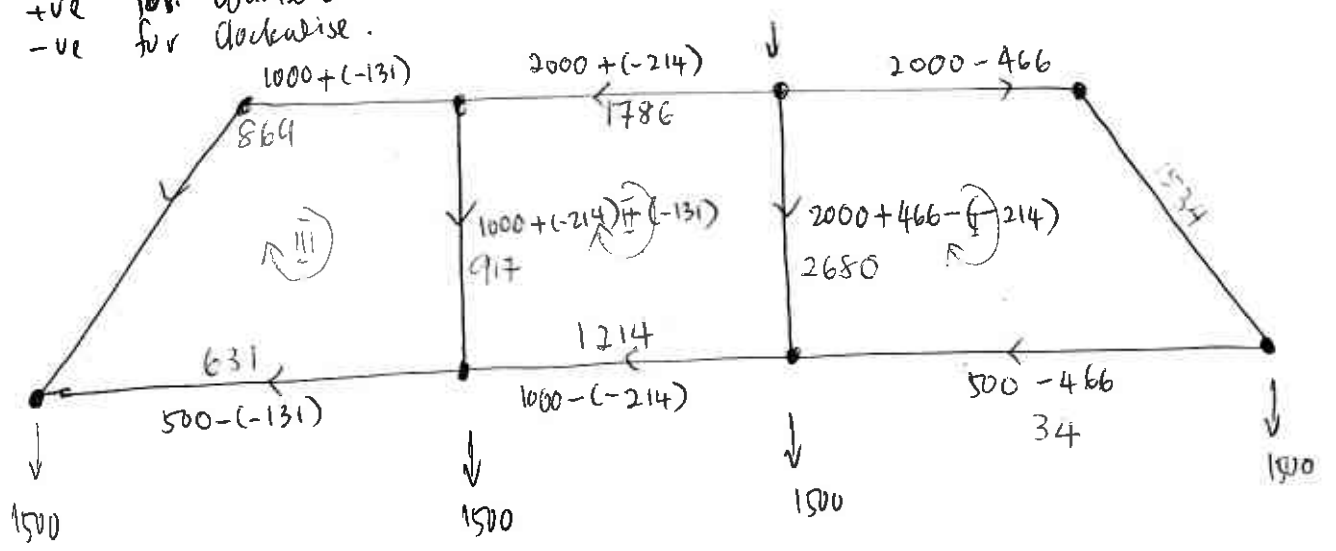
$$\therefore k_a, k_g = 5014$$

$$k_b, k_c, k_d, k_h = 4178.5$$

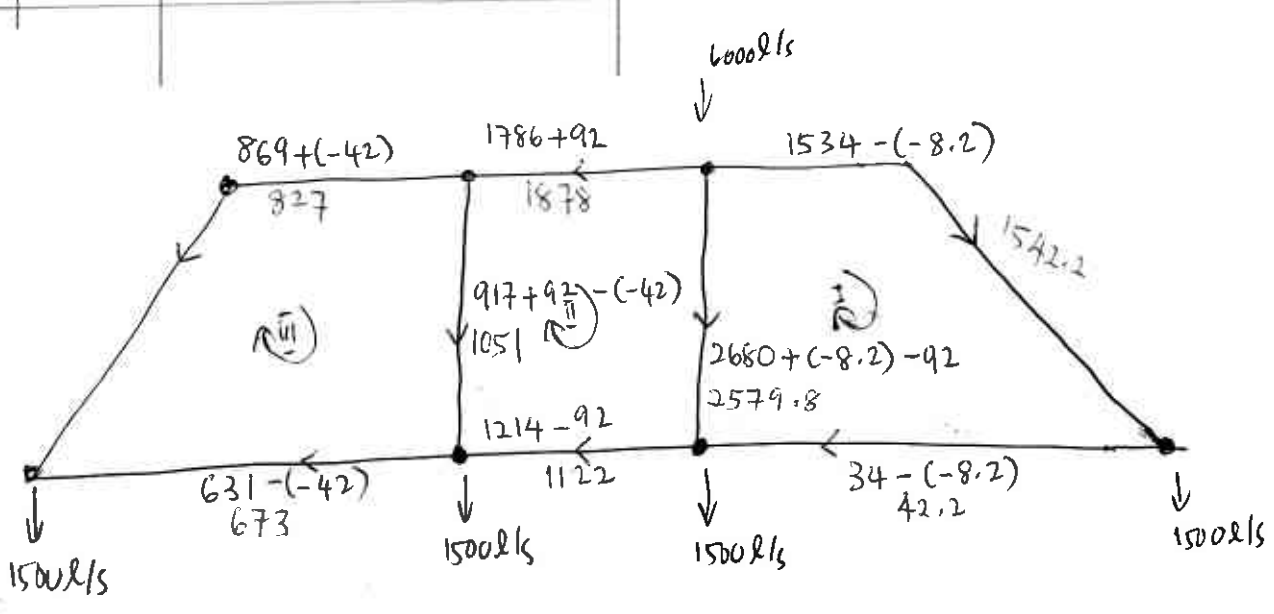
$$k_c, k_f = 1671.38$$

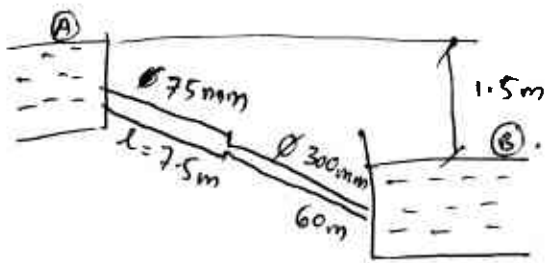
loop	Pipe	$\sum K_c Q_c^2 - \sum K_{cc} Q_{cc}^2$	$2\sum K_c Q_c + \sum K_{cc} Q_{cc}$
I	(a)	$(5014)(2)^2 = 20056$	$2(5014)(2) = 20056$
	(b)	$(4178.5)(0.5)^2 = 1044.5$	$2(4178.5)(0.5) = 4178.5$
	(c)	$-(1671.38)(2)^2 = -6685.52$	$2(1671.38)2 = 6685.52$
		14414.98	30920.02
			$\delta Q = \frac{14414.98}{30920.02} = 0.466 \text{ m}^3/\text{s}$ 466 l/s.
II	(c)	$(1671.38)(2)^2 = 6685.52$	$2(1671.38)2 = 6685.52$
	(d)	$-(4178.5)(2)^2 = -16714$	$2(4178.5)2 = 16714$
	(e)	$(4178.5)(1)^2 = 4178.5$	$2(4178.5)(1) = 8357$
	(f)	$-(1671.38)(1)^2 = -1671.38$	$2(1671.38)(1) = 3342.76$
		-7521.36	35099.28
			$\delta Q = \frac{-7521.36}{35099.28} = -0.214 \text{ m}^3/\text{s} @ -214 \text{ l/s}$
III	(f)	$1671.38(1)^2 = 1671.38$	$2(1671.38)(1) = 3342.76$
	(g)	$-5014(1)^2 = -5014$	$2(5014)(1) = 10028$
	h	$4178(0.5)^2 = 1044.5$	$2(4178)(0.5) = 4178$
		-2298.12	17548.76
			$\delta Q = \frac{-2298.12}{17548.76} = -0.131 \text{ m}^3/\text{s} @ 131 \text{ l/s}$

+ve for Counterclockwise
-ve for Clockwise.



loop	Pipe	$\sum k_c Q_c^2 - \sum k_{cc} Q_{cc}^2$	$2 \sum k_c Q + k_{cc} Q_{cc}^2$
I	Ⓐ	$(5014)(1.534)^2 = 11798.7$	$2(5014)(1.534) = 15382.95$
	Ⓑ	$(4178.5)(0.034)^2 = 4.83$	$2(4178)(0.034) = 284.104$
	Ⓒ	$-(1671.38)(2.68)^2 = -12004.5$	$2(1671.38)(2.68) = 8958.59$
		-200.99	24624.7
			$\delta Q = \frac{-200.99}{24624.7} = -8.163 \times 10^{-3} \text{ m}^3/\text{s}$ Ⓐ -8.2 l/s.
II	Ⓒ	$1671.38(2.68)^2 = 12004.5$	$2(1671.38)(2.68) = 8958.59$
	Ⓓ	$-(4178.5)(1.786)^2 = -13328.6$	$2(4178.5)(1.786) = 14925.6$
	Ⓔ	$(4178.5)(1.214)^2 = 6158.3$	$2(4178.5)(1.214) = 10145.4$
	Ⓕ	$-(1671.38)(0.917)^2 = -1405.4$	$2(1671.38)(0.917) = 3065.3$
		3428.8	37094.5
			$\delta Q = \frac{3428.8}{37094.5} = 0.092 \text{ m}^3/\text{s}$ Ⓓ 92 l/s.
III	Ⓕ	$1671.38(0.917)^2 = 1405.4$	$2(1671.38)(0.917) = 3065.3$
	Ⓖ	$-(5014)(0.869)^2 = -3786.4$	$2(5014)(0.869) = 8714.3$
	Ⓗ	$4178(0.631)^2 = 1663.5$	$2(4178)(0.631) = 5272.6$
		-717.5	17052.2
			$\delta Q = \frac{-717.5}{17052.2} = -0.042 \text{ m}^3/\text{s}$ Ⓕ -42 l/s.





$$f = 0.002(1 + 25/d)$$

$$= 0.002 + 0.05/d$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\rho g} + z_B + \frac{V_B^2}{2g} + \sum \text{Losses}_{(AB)}$$

$$z_A - z_B = \sum \text{Losses}_{(AB)}$$

$$(1.5 - 0) = \sum \text{Losses}_{(AB)}$$

$$\sum \text{Losses}_{AB} = K Q^2 + K Q^2$$

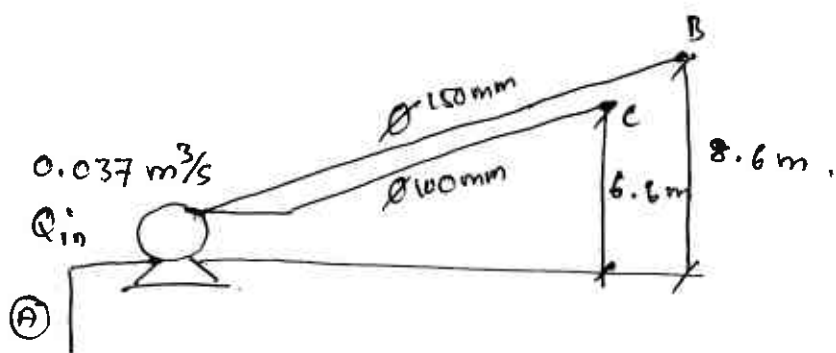
$$\sum \text{Losses} = \frac{16f_1 l_1}{2g \pi^2 d^5} Q^2 + \left(\frac{16f_2 l_2}{2g \pi^2 d^5} \right) Q^2$$

$$\sum \text{Losses} = \frac{16(0.002 + 0.05/d)(7.5)}{2g \pi^2 d^5} Q^2 + \frac{16(0.002 + 0.05/d)60}{2g \pi^2 d^5} Q^2$$

$$\sum \text{Losses} = \frac{74.62 \times 10^3}{11.403 \times 10^3} Q^2 + 25.332 Q^2$$

$$1.5 = 11428.52 Q^2$$

$$Q = 0.0115 \text{ m}^3/\text{s}$$



$$f = 0.032$$

$$Q_A = Q_B + Q_C$$

$$\sum \text{loss}_B = \sum \text{loss}_C$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A + H_p = \frac{P_B}{\rho g} + \frac{V_B^2}{2g} + z_B + \sum \text{loss}_{(A,B)}$$

guess Q_B as $0.017 \text{ m}^3/\text{s}$.

$$Q = AV$$

$$V = \frac{4Q}{\pi d^2}$$

$$V = 0.962 \text{ m/s}$$

$$\begin{aligned} \sum \text{loss}_B &= \left(\frac{fL}{d}\right) \frac{V^2}{2g} \\ &= \frac{(0.032)(45)}{0.15} \left(\frac{0.962^2}{2g}\right) \end{aligned}$$

$$\sum \text{loss}_B = 0.604$$

$$\sum \text{loss}_B = \frac{f_c L_c}{d_c} \left(\frac{V_c^2}{2g}\right)$$

$$0.604 = \frac{(0.032)(45)}{0.1} \frac{V_c^2}{2g}$$

$$0.604 = \frac{(0.032)(45)}{0.1} \frac{V_c^2}{2g}$$

$$V_c = 0.91 \text{ m/s}$$

$$Q_c = \frac{\pi d^2}{4} V$$

$$= 0.00712 \text{ m}^3/\text{s}$$

Take a ratio Q_B/Q_C .

$$Q_B = \left(\frac{Q_B'}{Q_B' + Q_C'} \right) Q_A = 0.0261 \text{ m}^3/\text{s}.$$

$$Q_C = \left(\frac{Q_C'}{Q_B' + Q_C'} \right) 0.037 = 0.0109 \text{ m}^3/\text{s}.$$

$$\frac{P_A}{\rho g} + \frac{V_A^2}{2g} + z_A + H_p = \frac{P_B}{\rho g} + \frac{z_B^2}{2g} + z_B + \sum \text{loss}_{AB}$$

$$H_p = (z_B - z_A) + \sum \text{loss}.$$

$$H_p = 8.5 + 0.604$$

$$H_p = 9.204 \text{ Watt}.$$